

gamsworldqformulation

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1 Optimization Models and MCP Formulation

Optimization Models

Here is the firm's problem. Since we have two firms there would be one for each firm:

$$\begin{array}{ll}
 \max & (\lambda^{DA} + \rho) * g_i^{DA} + \rho * e_i + \lambda^{RT} * (g_i^{RT} - g_i^{DA}) - C g_i^{RT} - (\lambda^{RT} - K) * e_i \\
 \text{s/t} & g_i^{DA} \leq Q_i^{DA} \\
 & g_i^{RT} \leq Q_i^{RT} \\
 & e_i \leq Q_i^{EIR}
 \end{array}
 \begin{array}{l}
 [\delta_i] \\
 [\gamma_i] \\
 [\zeta_i]
 \end{array}$$

The day ahead problem:

$$\begin{array}{ll}
 [EDDA] & \min \sum_i (C \hat{g}_i^{DA} + R_i \hat{e}_i) \\
 \text{s/t} & \hat{g}_i^{DA} \leq Q_i^{DA} \quad [u_i] \\
 & \hat{e}_i \leq Q_i^{EIR} \quad [\epsilon_i] \\
 & \sum_i \hat{g}_i^{DA} = D^{DA} \quad [\lambda^{DA}] \\
 & \sum_i \hat{g}_i^{DA} + \sum_i \hat{e}_i = FER \quad [\rho]
 \end{array}$$

The real time problem is identical to the no option formulation:

$$\begin{array}{ll}
 [EDRT] & \min \sum_i C \hat{g}_i^{RT} \\
 \text{s/t} & \hat{g}_i^{RT} \leq Q_i^{RT} \quad [v_i] \\
 & \sum_i \hat{g}_i^{RT} = D^{RT} \quad [\lambda^{RT}]
 \end{array}$$

MCP

$$\begin{array}{l}
 0 \leq C_i - \lambda^{DA} - \rho - \delta_i \perp g_i^{DA} \geq 0 \\
 0 \leq R_i - \rho - \zeta_i \perp e_i \geq 0 \\
 0 \leq C_i - \lambda^{RT} - \gamma_i \perp g_i^{RT} \geq 0 \\
 0 \leq Q_i^{DA} - g_i^{DA} \perp \delta_i \geq 0 \\
 0 \leq Q_i^{RT} - g_i^{RT} \perp \gamma_i \geq 0 \\
 0 \leq Q_i^{EIR} - e_i \perp \zeta_i \geq 0 \\
 \sum_i g_i^{DA} + \sum_i e_i = FER \\
 \sum_i g_i^{DA} = D^{DA} \\
 \sum_i g_i^{RT} = D^{RT}
 \end{array}$$